Molecular dynamics simulation of structural changes of lipid bilayers induced by shock waves: Effects of incident angles

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ABSTRACT

Unsteady and nonequilibrium molecular dynamics simulations of the response of dipalmitoylphosphatidylcholine (DPPC) bilayers to the shock waves of various incident angles are presented. The action of an incident shock wave is modeled by adding a momentum in an oblique direction to water molecules adjacent to a bilayer. We thereby elucidate the effects of incident shock angles on (i) collapse and rebound of the bilayer, (ii) lateral displacement of headgroups, (iii) tilts of lipid molecules, (iv) water penetration into the hydrophobic region of the bilayer, and (v) momentum transfer across the bilayer. The number of water molecules delivered into the hydrophobic region is found to be insensitive to incident shock angles. The most important structural changes are the lateral displacement of headgroups and tilts of lipid molecules, which are observed only in the half of the bilayer directly exposed to a shock wave for all incident shock angles studied here. As a result, only the normal component of the added oblique momentum is substantially transferred across the bilayer. This also suggests that the irradiation by shock waves may induce a jet-like streaming of the cytoplasm toward the nucleus.

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1. Introduction

The cell membrane permeabilization technique utilizing mechanical forces due to high-intensity acoustic waves (shock wave or ultrasound) is a promising method of noninvasive drug and gene delivery into the cytoplasm [1–5]. For the last decade, several authors have addressed the permeabilization mechanisms, in vitro and in vivo, which are fundamental for the complete development of drug and gene delivery methods based on shock waves or ultrasound [6–14]. They have reported that cavitation-induced nonthermal effects (e.g., radiation force, micro-streaming, micro-jets, or shock waves from cavitation bubbles) can induce reversible lesions of cell membranes, and the cell membranes are thereafter permeabilized [6–14].

The above mentioned studies are limited to the macroscopic or cellular level. At the microscopic or molecular level, on the other hand, the mechanisms of the permeabilization induced by shock waves or ultrasound are not well understood. Recently, we conducted molecular dynamics (MD) simulations of the structural changes of phospholipid bilayers of cell membranes induced by the action of shock waves [15]. One of the important findings was that the resulting collapse and rebound of a bilayer are followed by the penetration of water molecules into the hydrophobic region of the bilayer.

In the simulations, the propagation direction of the applied incident shock waves was parallel to the bilayer normal direction. However, bilayers are generally undulating on a length scale well beyond their thickness [16]. That is, the incident shock angles on the membrane surface practically vary with the location on the surface where the shock wave impacts. Furthermore, a numerical analysis in fluid dynamics [17] points out that an oblique impact of a shock wave induces a kind of shear flow around cell membranes and the forces resulting from the flow field are responsible for cell deformation and lysis. The effects of the incident shock angles on the structural changes of lipid bilayer underneath the permeabilization mechanisms at the molecular level. Therefore, the objective of this study is to analyze the structural changes of lipid bilayer by using the shock waves of various incident shock angles.

The foundation of all biological membranes is the lipid bilayer structure consisting of two leaflets of phospholipids. Thus, their dynamics (i.e., rearrangement of the phospholipids) is central to understanding the behavior of biological membranes. MD simulations of lipid bilayers have provided accurate models of biological membranes at the nanometer and nanosecond scales [18–21], and the molecular behaviors of lipids, water, and membrane proteins in equilibrium states have been clarified [18,22–25]. Moreover, the studies on the lipid bilayer responses to surface area changes [26], mechanical stresses [27], electric fields [28–30], and shear flows [31–33] are beginning to be conducted.
However, these studies involve responses in the steady or almost steady states. We emphasize that a shock wave is a high-pressure wave with a steep wave front that propagates at a supersonic speed, and it passes the cell membrane within a very short time of the order of picoseconds. Therefore, understanding the high-speed phenomenon induced by the interaction of a shock wave with a lipid bilayer should be indispensable. We address the lipid bilayer responses not to steady but unsteady actions induced by shock waves, particularly focusing on the effect of various incident shock angles.

In the previous study [15], we have modeled a shock wave by its impulse and performed unsteady and nonequilibrium MD simulations. Here, we slightly modify the shock wave impulse model to take account of incident shock angles, and the modified model is described in the Methods section. In the Results section, the collapse stage and the rebound stage are defined, and then the lateral displacement of headgroups, tilts of lipid molecules, water penetration into the hydrophobic region of a bilayer, and the momentum transfer across the bilayer are analyzed in detail. We finally summarize the effects of incident shock angles on the structural changes of a bilayer and discuss possible streaming in the cytoplasm induced by shock waves in the Summary and discussion section.

2. Methods
2.1. Lipid bilayer system

In this study, we investigated the effect of the incident angle of a shock wave on a lipid bilayer distributed on a plane surface (see Fig. 1). The lipid bilayer system comprised 128 DPPC molecules fully hydrated by 16455 water molecules. For equilibration, we performed 20-ns simulations with our force fields (see below) in a constant NPT ensemble, and we obtained the equilibrated bilayer system of volume \( V = 6.56 \times 10^{-3} \) nm\(^3\), where the linear dimension of the simulation box in the \( z \) direction normal to the bilayer plane (the \( xy \) plane) is 15.90 nm. The detailed simulation procedures for the bilayer equilibration are summarized elsewhere [15,19]. We remark that our system included a large water layer of thickness about 12 nm, whereas the thickness of the bilayer was about 4 nm. This is because this simulation of a shock wave required a large number of water molecules, as explained below.

The force fields for DPPC and water were consistent with those employed in the previous study [15], which includes the refined united atom force field with AMBER99 force field [19] and single point charge (SPC) model [34]. The partial charges of a DPPC molecule were obtained from the study by Chiu et al. [35]. Because we are interested in the dynamical process of a structural change in a bilayer resulting from shock wave irradiation, it may be better to remove the constraints of molecular bond lengths, angles, and dihedrals. Therefore, all bonded interactions in DPPC molecules were calculated in the shock wave simulation. The particle mesh Ewald method [36] was used to treat the long-range electrostatic interactions. Both the real-space Ewald and the van der Waals nonbonded interactions were cut off at 1.0 nm. The AMBER 8 set of programs [37] was used for computations.

2.2. Shock wave impulse simulation

As demonstrated in the previous study [15], we modeled a shock wave by its impulse \( I \) defined as the time integral of pressure over the shock-pulse duration [7]. From the definition of the impulse, the shock impulse \( I \) can be regarded as an increment in the momentum of water divided by an area \( A \) on which the shock pressure is exerted. The momentum increment is numerically implemented by the addition of the average velocity \( V \) to the thermal velocity of water molecules in a slab adjacent to a bilayer. \( V \) is given by

\[
V = \frac{I}{mN_w},
\]

where \( m \) is the weight of a water molecule and \( N_w \) is the number of water molecules in the water slab.

Because the choice of a water slab is arbitrary, we consider the water slab of \( A \times L_w \) where \( A = 42.2 \text{ nm}^2 \) was the area of the \( xy \) plane of the bilayer system and \( L_w = 4.0 \text{ nm} \) was the thickness of the water slab. We set \( I = 40 \text{ mPa s} \) and the number of water molecules in the water slab \( N_w = 5423 \); the applied average velocity \( V \) was 10.394 m/s. Note that \( V \) corresponds neither to the sound speed in liquid water nor to the propagation speed of the shock wave. It just represents the increase in the momentum of water molecules due to the shock wave.

In the present study, we slightly modified the shock wave model described above to take account of the incident shock angle. More precisely, the shock wave impulse was divided into the normal (in the \( z \) direction) and tangential (in the \( x \) direction) components to the bilayer plane (see Fig. 1). That is,

\[
I_z = I \cos \theta \quad \text{and} \quad I_t = I \sin \theta,
\]

where \( I_z \) is the normal component; \( I_t \), the tangential component; and \( \theta \), the incident shock angle. \( V \) was decomposed to the normal component \( V_z = \frac{I_z}{mN_w} \) and the tangential component \( V_t = V \sin \theta \).

For understanding high-speed and unsteady phenomenon induced by a shock wave impulse in MD, position and velocity scaling of molecules should not be implemented. Therefore, we performed constant NVE MD simulation without using the temperature and pressure controls and bond constraints from the initial configuration. The constant energy in this MD is the sum of the total energy in the equilibrium state and the kinetic energy increase induced by adding velocity. Periodic boundary conditions were applied in the three directions. The time step used for the integration of equations of motion was 0.2 fs in order to avoid the excess approach of molecules with large velocities. Owing to the periodic boundary conditions, the simulations were terminated at the time when the effect of the shock impulse reached the boundary at the opposite side of the simulation box in the \( z \) direction. This is the reason why we prepared a thick water layer. The numerical results shown in the following are the sample averages of 10 production runs for a given \( \theta \). From the results of the previous study and preliminary calculations, the system size and the simulation time in the present study were determined in order to focus on the analysis of the essential part of the structural changes in unsteady states.

![Fig. 1. Schematic diagram of the interaction of a shock wave with a lipid bilayer, where \( \theta \) is the incident angle between the bilayer normal and the direction of shock wave propagation.](image)

![Fig. 2. Temporal changes of the bilayer thickness in the simulations for \( \theta = 0^\circ, 30^\circ, \) and \( 60^\circ \). The bilayer thickness is normalized by that in the initial state (ca. 4.0 nm). Note that in the following figures the normalized time \( t^* = 1 \) corresponds to 530, 590, and 810 fs in real time for \( \theta = 0^\circ, 30^\circ, \) and \( 60^\circ \), respectively.](image)
2. Analysis

The changes of hydrophobic chains in the unsteady states can be explained in terms of an averaged instantaneous chain order parameter $S_{CD}$ [15],

\[
S_{CD}(t) = \frac{1}{2} \left( \frac{1}{N_L} \sum_{i=1}^{N_L} \frac{1}{2} (3 \cos^2 \theta_i - 1) \right) + \frac{3}{2} \left( \frac{1}{N_L} \sum_{i=1}^{N_L} \sin \theta_i \right),
\]

where $\theta_i$ is the angle between the axis of the $i$th molecular axis and the bilayer normal (the $z$ axis) and $N_L (=28)$ is the number of carbons in both sn-1 and sn-2 chains. $\theta_i$ is evaluated from the instantaneous configurations of lipid molecules. Note that $\theta_i$ in the upper layer is calculated with respect to the bilayer director as pointed out in Ref. [31], because the lipid molecules in the upper layer tilt (see the Results section).

The lateral movement of lipid molecules is characterized by the averaged lateral displacement of the mass center positions of the headgroups of lipid molecules $L(t)$ defined by

\[
L(t) = \frac{1}{N_L} \sum_{i=1}^{N_L} |x_i(t) - x_i(0)|,
\]

where $x_i$ is the $x$ coordinate of the mass center position of the headgroup of the $i$th molecule, and $N_L (=64)$ is the number of DPPC molecules in the upper or lower layer.

3. Results

3.1. Collapse and rebound of bilayers

The most outstanding change in a bilayer by the action of a shock wave is the change in the bilayer thickness, which is defined as the distance between the phosphorus atoms of lipid molecules in the upper and lower layers [15]. Fig. 2 shows the temporal changes of the bilayer thickness caused by the shock wave impulses of 40 mPa·s for $\theta=0^\circ$, 30°, and 60°. The bilayer thickness became minimum at 530, 590, and 810 fs for $\theta=0^\circ$, 30°, and 60°, respectively. The normalized time $t^* = \frac{t}{t_{uni}}$ in Fig. 2 is defined such that the minimum of bilayer thickness occurs at $t^* = 1$. That is, the bilayer thickness is decreasing during $0 < t^* < 1$ (i.e., collapse stage); then, the bilayer thickness starts to increase after $t^* = 1$ (i.e., rebound stage) regardless of the incident shock angle conditions. In the following the normalized time $t^* = 1$ corresponds to 530, 590, and 810 fs in real time for $\theta=0^\circ$, 30°, and 60°, respectively.

In each incident angle condition, the duration of the rebound stage ($1 < t^*$) is longer than that of the collapse stage ($0 < t^* < 1$). The rebound stage was not completed within the present simulation because of the periodic boundary conditions (see the Methods section). However, the essential points can be clarified as demonstrated below.

The change in the bilayer thickness is expected to be due to the postural changes of lipid molecules. In Fig. 3, we show a series of snapshots of postural changes of typical lipid molecules in the upper and lower layers induced by the shock wave with $\theta=60^\circ$. By the action of the shock wave, the hydrophobic chains bend (Fig. 3(a)-(c)) and then slightly recover (Fig. 3(d) and (e)). Fig. 4 shows temporal changes of $S_{CD}$ for $\theta=60^\circ$, normalized by those in the initial state (ca. $-0.16$). The order parameters obviously decrease in the collapse stage and gradually recover in the rebound stage. On comparison with the result in Fig. 2, it is confirmed that the decrease in the bilayer thickness was due to this chain disorder. This result is consistent with the previous simulation result [15].

3.2. Lateral movement of lipid molecules

The oblique incidence of a shock wave yields unsteady shear on the bilayer surface. In this simulation, the shear is induced by the tangential momentum change of water molecules adjacent to the bilayer surface (see the Methods section). In Fig. 3, the effect of shear appears as the lateral movement of the lipid molecules in the upper layer. Fig. 5 shows the time evolution of the averaged lateral displacements in the upper and lower layers. As pointed out in the previous study [15], the simple shock wave interaction ($\theta=0^\circ$) enhances the lateral displacement. However, the displacement in the upper layer significantly increases with the incident shock angle from $0^\circ$ to $60^\circ$. In fact, the displacement induced by the shock wave with $\theta=60^\circ$ becomes 1.5 nm at $t^* = 2$, which is ten times larger than that with $\theta=0^\circ$. Here, we remark that the lateral displacements of lipid molecules for $\theta=30^\circ$ and $60^\circ$ continue to increase even in the rebound stage. On the other hand, the lateral displacement in the lower layer is one order of magnitude smaller than that in the upper layer (Fig. 5 inset).

3.3. Tilt of lipid molecules

From the snapshots in Fig. 3, it is clear that the lipid molecule in the upper layer tilts by the action of incident shock wave. Here, we define the tilt angle as follows: (i) atom positions of a lipid molecule are projected onto the $xz$ plane; (ii) a straight line is fitted to these projected

![Fig. 3. Snapshots of postural changes of typical lipid molecules in upper and lower layers induced by the shock wave with $\theta=60^\circ$. The yellow bars represent the headgroup of a lipid molecule; the orange bars, the hydrophobic chains; and the red spheres, water molecules. The yellow arrow in the snapshot of $t^*=0$ denotes the propagation direction of the incident shock wave. The other lipid molecules are eliminated for clarity.](https://example.com/fig3.png)

![Fig. 4. Temporal changes of averaged instantaneous order parameter for $\theta=60^\circ$. The order parameters are normalized by those in the initial state.](https://example.com/fig4.png)
positions; (iii) the tilt angle $\theta$ is obtained from the angle formed between this straight line and the $z$ axis (see Fig. 3(e)). The tilt angle in the initial state ($t^*=0$) calculated here has a wide distribution centered around zero degree, which would be tantamount to that in the equilibrium state of another study [24] although they used a different force field and their tilt angle is defined as that between a vector formed by alternating carbon units along the lipid tails and the bilayer normal axis.

Fig. 6(a) shows the tilt angle distributions of the lipid molecules in the upper layer at $t^*=2$. In the case of $\theta=0^\circ$, the distribution of tilt angles is hardly changed from that in the initial state. On the contrary, the distributions for $\theta=30^\circ$ and $60^\circ$ shift to the positive side. In Fig. 6(b), we show the temporal changes of the tilt angles averaged for all lipid molecules in the upper layer. Obviously, the averaged tilt angles for $\theta=30^\circ$ and $60^\circ$ increase with time and reach maximum values at around $t^*=2$ ($21^\circ$, and $32^\circ$, respectively). The maximum values are in agreement with those in Ref. [31] on the interaction of steady shear flows with lipid bilayers. In the present unsteady simulation, the lipid alignment is completed within $t^*=2$. Thus, the simulation limited to $0<t^*<2.0$ is adequate to analyze the essential part of the structural changes in unsteady states. Interestingly, whereas the lateral movement of lipid molecules persists as shown in Fig. 5, their tilts are saturated (Fig. 6(b)). However, this will not be discussed in this paper.

The tilt angles averaged in the lower layer did not change (data not shown). We emphasize that this is not due to the restriction of simulation time because the steady simulation of shear flow also obtained the same result [31].

3.4. Water penetration into the hydrophobic region

In the equilibrium state water molecules hardly exist in the hydrophobic region [18] and the event of water penetration into the hydrophobic region rarely occurs in the time scale of MD simulations [38,39]. On the other hand, under the action of shock waves the water penetration into the hydrophobic region was observed in the time scale of picoseconds (see Fig. 3), which is important for subsequent water pore formation in a bilayer [40] and cell membrane permeabilization [4,6,9,15]. Fig. 7 shows the temporal changes of the number of water molecules delivered into the hydrophobic region for $\theta=0^\circ$, $30^\circ$, and $60^\circ$. Here, the hydrophobic region is defined as the region between the carbonyl groups in $sn$-1 chains in the upper and lower layers [15]. Most of the water molecules penetrated are from the upper water layer. The water penetration in the intermediate stage of

![Fig. 5](link) Lateral displacement of the mass center of lipid headgroups for $\theta=0^\circ$, $30^\circ$, and $60^\circ$ in the upper layer and that in the lower layer (inset).

![Fig. 6](link) (a) Tilt angle distributions of the lipid molecules in the upper layer for $\theta=0^\circ$, $30^\circ$, and $60^\circ$ at $t^*=2.0$ (b) Temporal changes of the averaged tilt angle of lipid molecules in the upper layer. Note that the average equilibrium angle in the initial state is taken as $0^\circ$ in (b).

![Fig. 7](link) Number of the water molecules delivered into the hydrophobic region of a bilayer induced by shock wave with $\theta=0^\circ$, $30^\circ$, and $60^\circ$.

![Fig. 8](link) Temporal changes of the momentum of the lower water layer in the $z$ direction (normal component) and that in the $x$ direction (tangential component, inset) for $\theta=60^\circ$. 
the intermonolayer friction coefficient, $b$, which is one of the measures of the intermonolayer friction coefficient in classical plasma membrane mechanics, is given by $b=F/A\Delta V$, where $F$ is the sliding force per unit of bilayer area and $A$ is the bilayer area. The difference in the impulse intensity in the normal direction. In the rebound stage, on the other hand, a large amount of the normal component remains very small. That is, only the normal component of the applied oblique impulse is transferred across the bilayer.

Finally, we discuss the possible streaming of the cytoplasm induced by shock waves. As shown in Fig. 8, the normal component of the applied momentum promptly transfers across the bilayer, whereas the tangential component hardly transfers. Here, let us assume a cell to be a sphere and a shock wave impulse is applied downward on the surface of the sphere (Fig. 9(a)). The intensity of the applied momentum along membrane normal is largest on the top of the sphere, and it is reduced to zero along the meridian of the sphere. Accordingly, the momentum distribution has a maximum (Fig. 9(b) right), which will result in the formation of a jet-like streaming in the cytoplasm. In reality, the cell membrane is usually undulating; hence, several momentum maxima with different directions may be produced beneath the membrane. Therefore, the streaming in the cytoplasm caused by the shock wave will be comprised of several jet-like flows emerged from several momentum maxima, and the entire flow pattern in the cytoplasm will become complex. The mixing or homogenization of plasmid [10] and fluorescein [7] throughout the cell cytoplasm appears to be enhanced by jet-like flows.

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