

# An atomistic approach to materials: structure of glassy alumina and the mechanical response of copper

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[www.gnm.cl](http://www.gnm.cl)

Université Paris-Sud, Orsay, Jan. 30, 2013

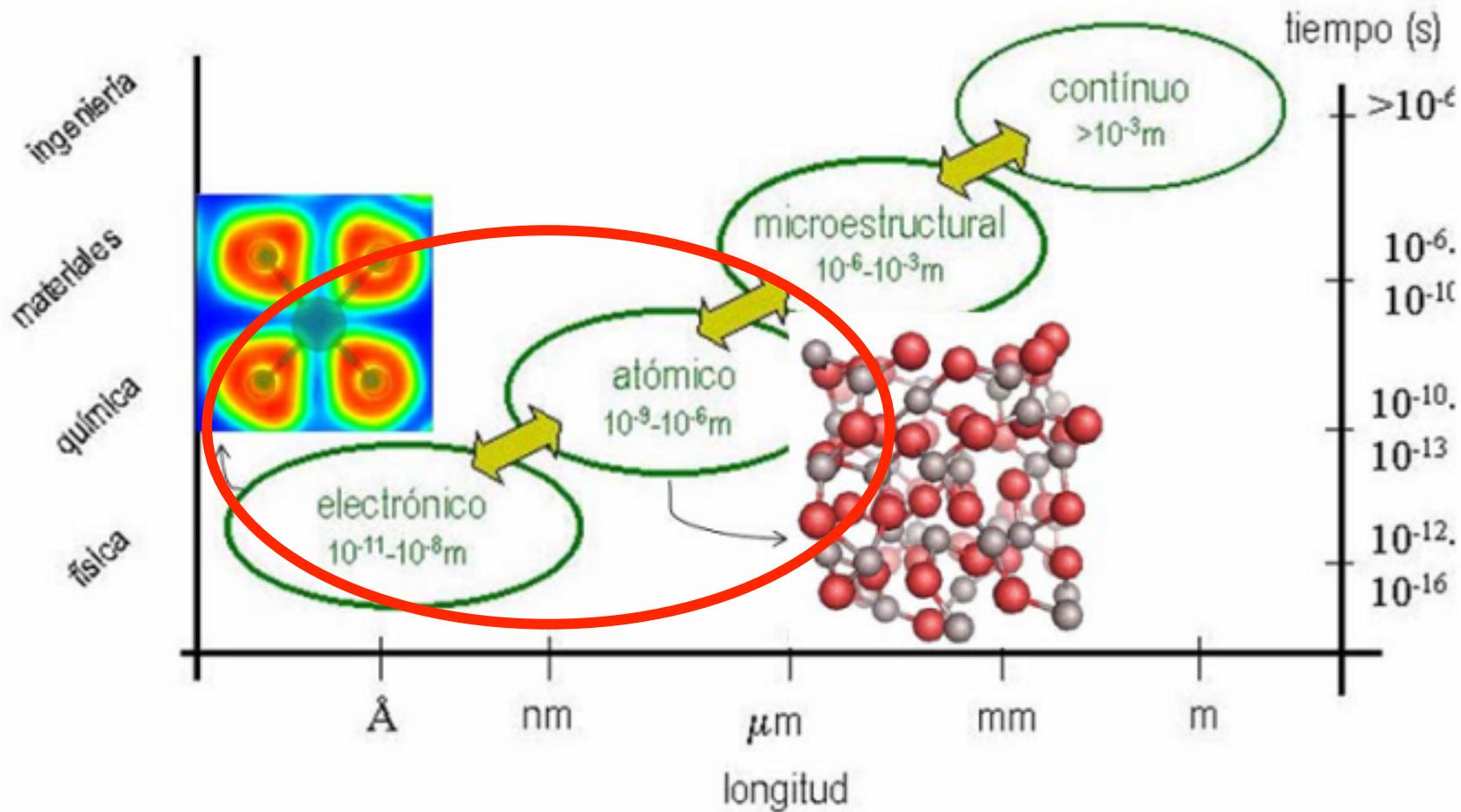
# Grupo de NanoMateriales, U. de Chile

[www.gnm.cl](http://www.gnm.cl)

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- Profs: Eduardo Menéndez, Sergio Davis, Gonzalo Gutiérrez
- Postdoc: Emilio Figueroa, Germán Miño
- Postgraduate students: F. González, Y. Navarrete, N. Amigo, E. Sánchez
- Approx. 10 undergrad per year
- Collaboration in Chile and abroad

# Atomistic simulation



# GNM: Research areas ([www.gnm.cl](http://www.gnm.cl))

## 1. Foundations of statistical mechanics:

- a) melting theory
- b) Information theory and bayesian probability
- c) non-extensive statistics

## 2. Material science

- a) glasses: structures, dynamical and mechanical properties
- b) nano-structured materials: carbon nanotubes
- c) materials under extreme conditions
- d) Mechanical properties of metals
- e) solar cell materials: electronic and optical properties (ab-initio)
- f) nuclear materials: radiation damage
- g) Biological systems: molecular simulation

## 3. Computer simulation techniques

- a) Computer programming: Las Palmeras Molecular Dynamics,  
[www.lpmdd.cl](http://www.lpmdd.cl) (Computer Physics Communications, 181(12):2126 – 2139, 2010)
- b) Free energy and entropy
- c) Algorithms for MD and MC: mpi, CUDA

# Outline

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- Molecular dynamics simulation
- Amorphous Al<sub>2</sub>O<sub>3</sub> by ab-initio MD
- Mechanical properties of copper by classical MD

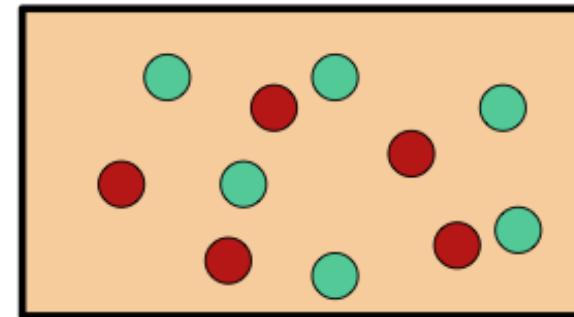
# Molecular Dynamics simulations

Inicial conditions:

$$\{\mathbf{r}_i(t_0), \mathbf{v}_i(t_0)\}_N$$



Choice of interatomic potential  $\Rightarrow$  forces



$$N \sim 2000$$
$$V$$
$$E_K = \frac{3}{2} N k_B T$$

- empirical pot
- ab-initio  $\epsilon(R)$

$$V(r) = \frac{q_i q_j}{r} - \frac{C_i C_j}{r^6} + B \exp(ar)$$

Numerical solution to the eqs. of motion

Verlet

$\Delta t: 10^{-15}$  s : time step

Physical properties: temporal average over configurations:  
 $\langle \dots \dots \rangle_t$

- Termodynamics prop.
- structural properties
- dynamical prop.

# Basic diagnostics

- Pair distribution function
- Angular distribution
- Coordination numbers
- Vibrational density of states  $D(w)$
- Direct visualization

*Average over positions,  
velocities and accelerations*

$$Z_{\alpha(\beta)}(t) = \left\langle \sum_{i=1}^N m_{i\alpha} \vec{v}_{i\alpha}(0) \cdot \vec{v}_{i\alpha}(t) \right\rangle \quad \text{VACF}$$

$$\mathcal{D}_{\alpha(\beta)}(\omega) = \frac{1}{\sqrt{2\pi}} \int \frac{Z_{\alpha(\beta)}(t)}{Z_{\alpha(\beta)}(0)} \exp(-i\omega t) dt$$

# Structural, elastic, vibrational, and electronic properties of amorphous Al<sub>2</sub>O<sub>3</sub> from ab-initio calculation\*

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**Ceramic material with several technological applications**

due to

high melting point (2327 K),  
extreme hardness (Moh 9) y  
low electrical conductivity

**Structural phase transitions**

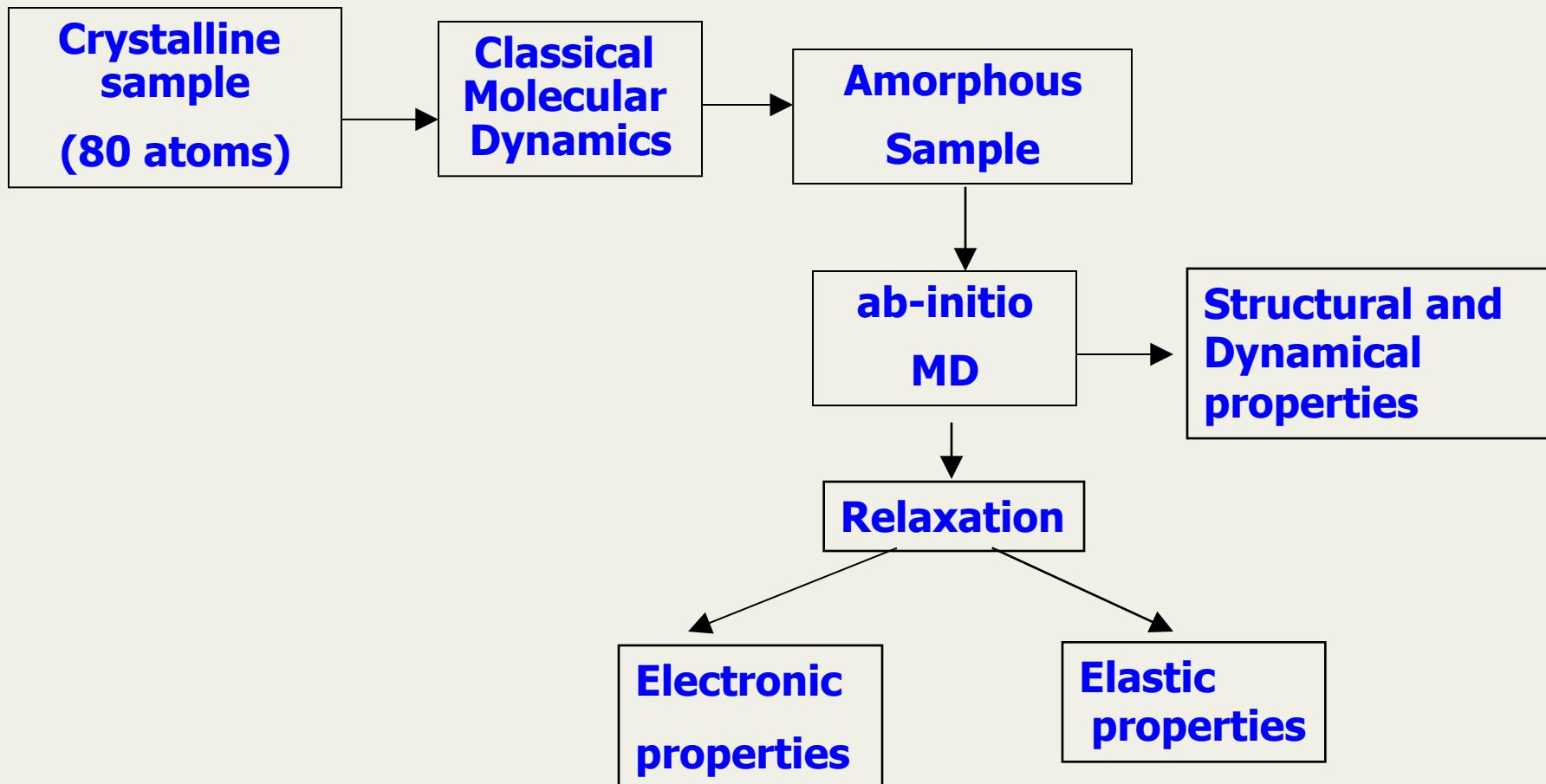
liquid  $\rightarrow \gamma \rightarrow \delta, \theta \rightarrow \alpha$ -alumina  
amorphous (a.o)  $\rightarrow \gamma \rightarrow \theta \rightarrow \alpha$ -alumina

**amorphous alumina? Not many experimental results**

\* S. Davis, G.G., J. Phys.: Condens. Matter 23, 495401 (2011)

# Procedure

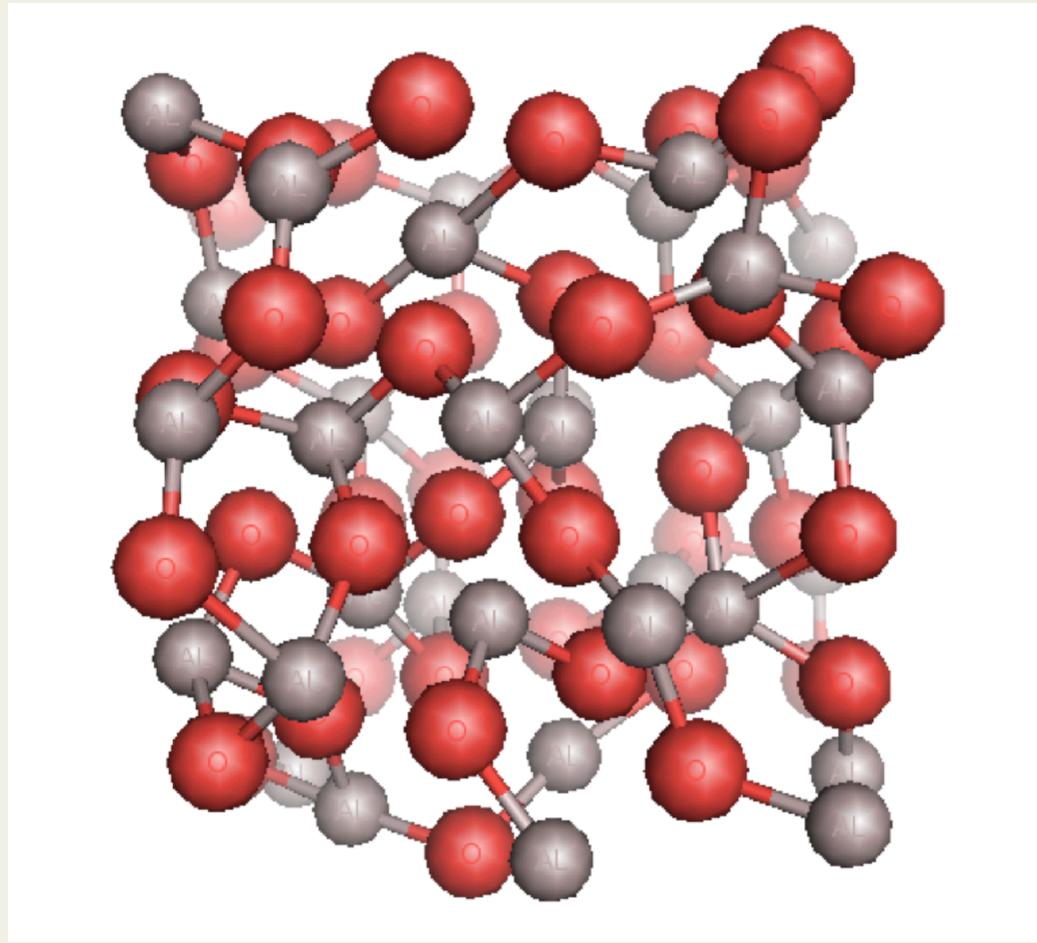
- Combined use of classical an *ab initio* Molecular Dynamics:



# Computational details

- *ab initio* MD by using VASP (Vienna Ab Initio Simulation Package)
- Density Functional Theory with LDA (local density approximation)
- Ultrasoft pseudopotentials
- Energy cutoff  $E_{cut} = 296,77$  eV (21,81 Ry)
- Only gamma point,  $\Gamma = (0,0,0)$
- Time step of 3 fs for atomic motion

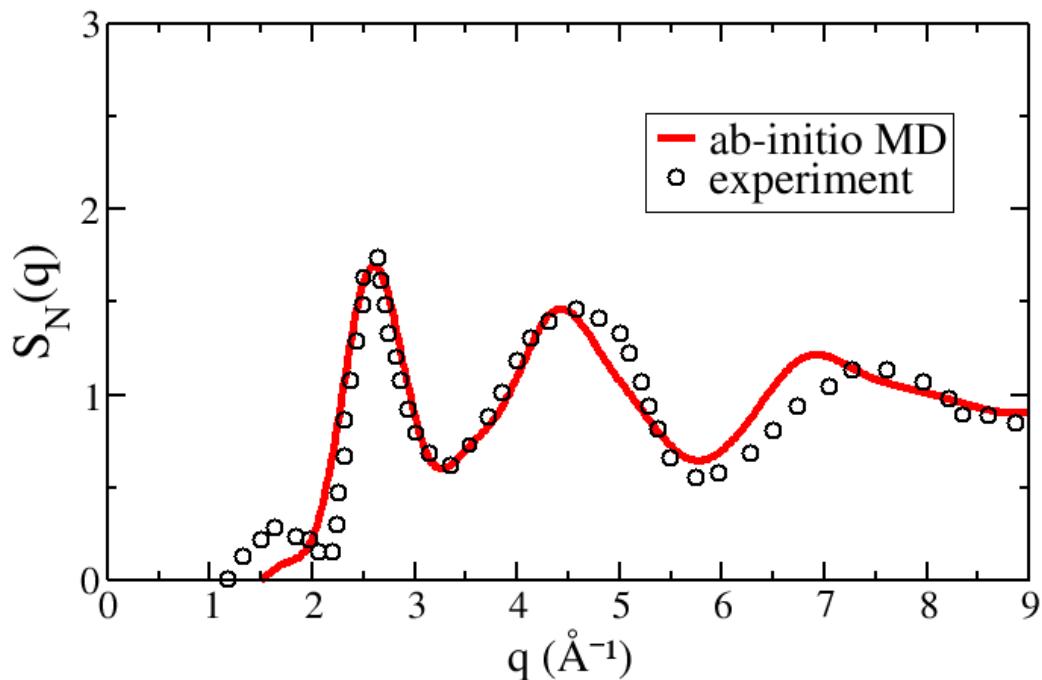
# Amorphous Al<sub>2</sub>O<sub>3</sub>



S. Davis, G. G,  
Structural, elastic, vibrational, and electronic properties of amorphous  
Al<sub>2</sub>O<sub>3</sub> from ab-initio calculations

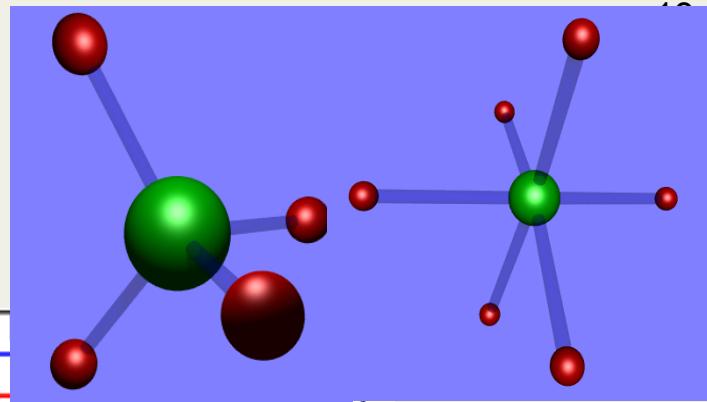
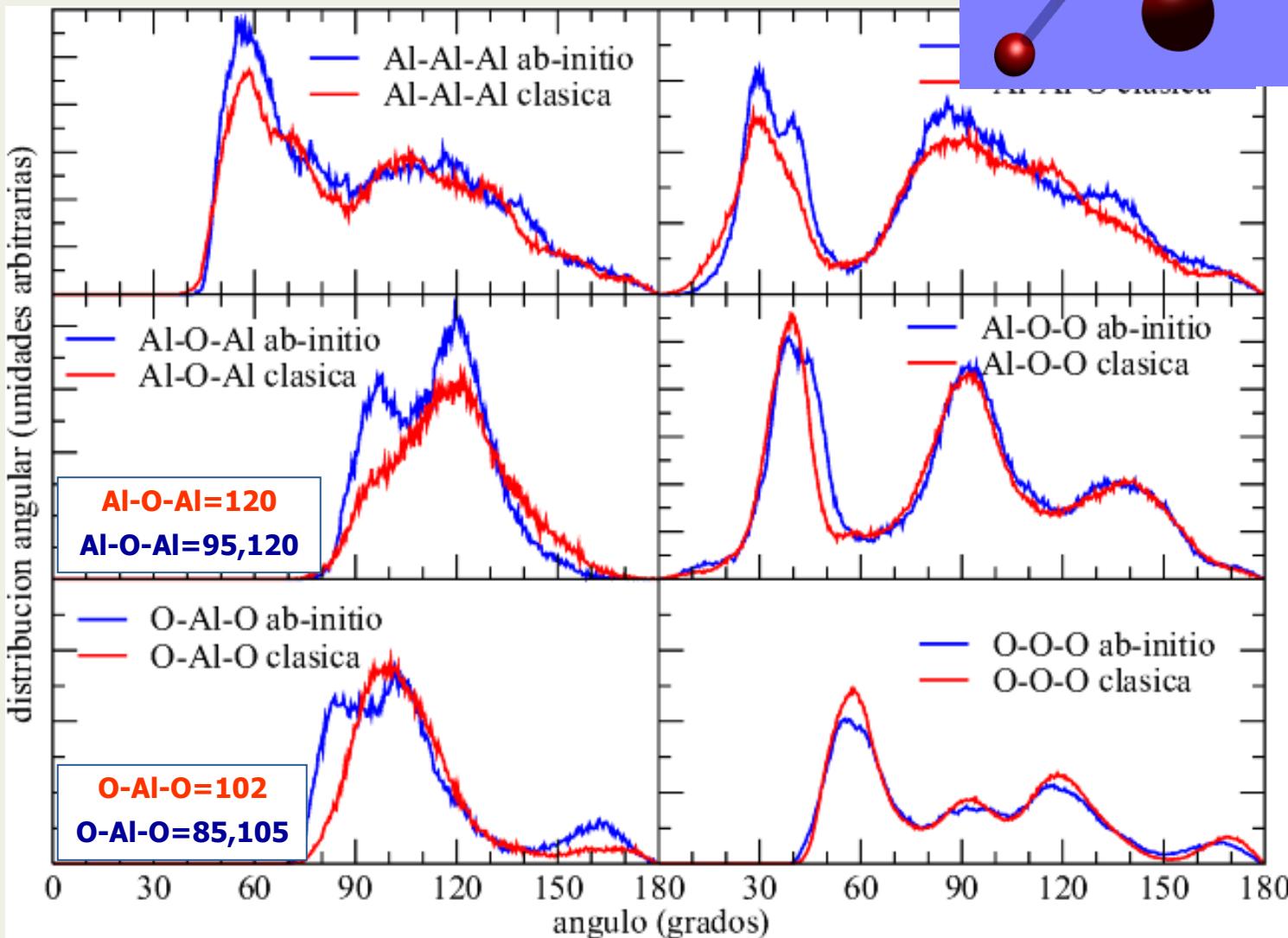
J. Phys.: Condens. Matter 23, 495401 (2011)

# Neutron static structure factor: experiments and simulation



Exp.:  
P. Lamperter,  
R. Kniep,  
Physics B **234**, 405 (1997)

# Angular distribution



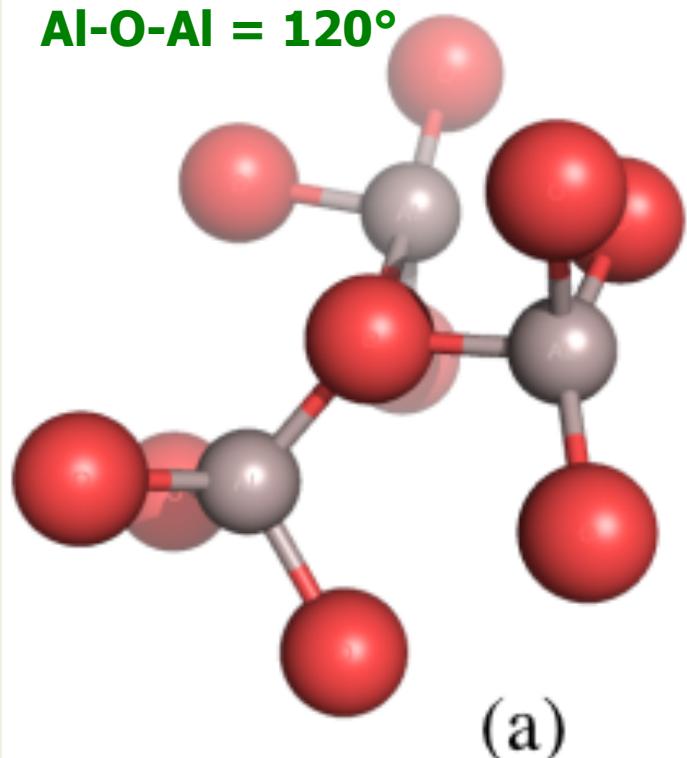
# Interatomic distances and coordination numbers

<b>Results</b>	<b>R<sub>Al-Al</sub> (Å)</b>	<b>R<sub>Al-O</sub> (Å)</b>	<b>R<sub>O-O</sub> (Å)</b>
Lamparameter y Kniep	$3,2 \pm 0,55$	$1,8 \pm 0,21$	$2,8 \pm 0,58$
Cassical MD	3,24	1,74	2,77
<i>ab initio</i> MD	3,27	1,80	2,91

<b>Results</b>	<b>n<sub>Al-Al</sub></b>	<b>n<sub>Al-O</sub></b>	<b>n<sub>O-Al</sub></b>	<b>n<sub>O-O</sub></b>
Classical MD	9,1	3,97	2,65	16,85
<i>ab initio</i> MD	8,9	4,49	2,99	16,46

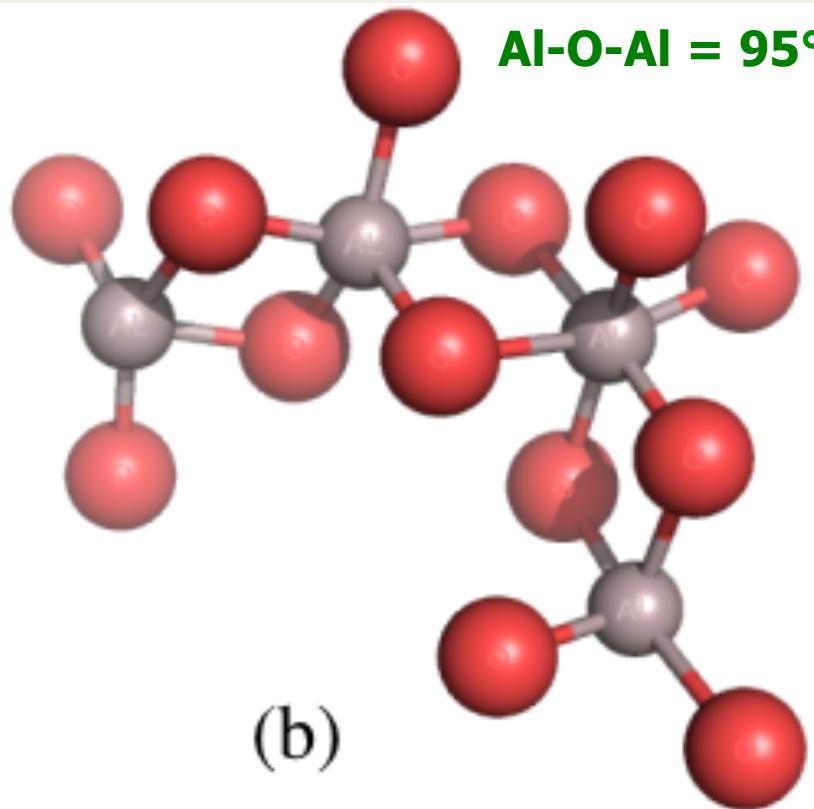
# Connectivity between basic units

**Al-O-Al = 120°**



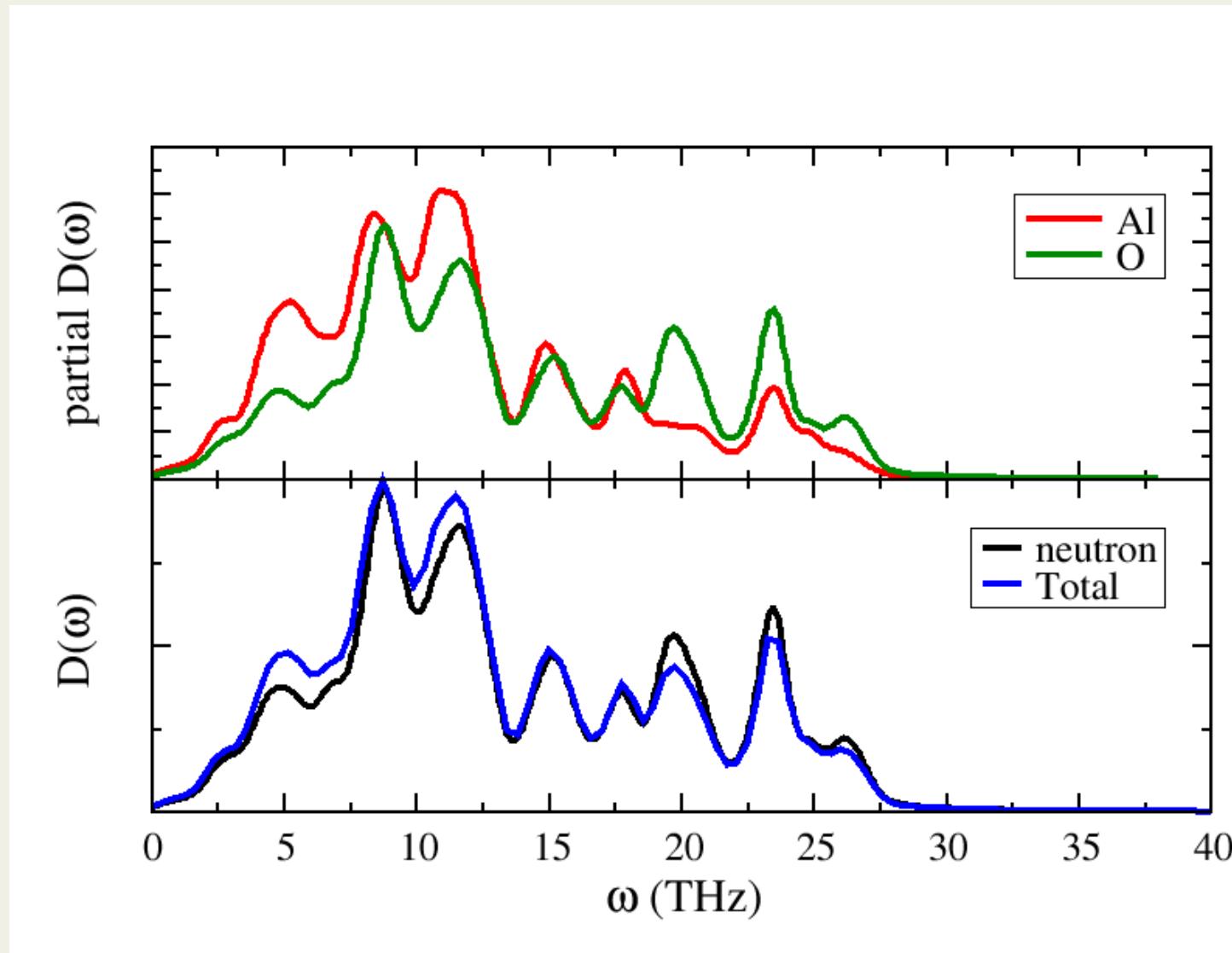
(a)

**Al-O-Al = 95°**

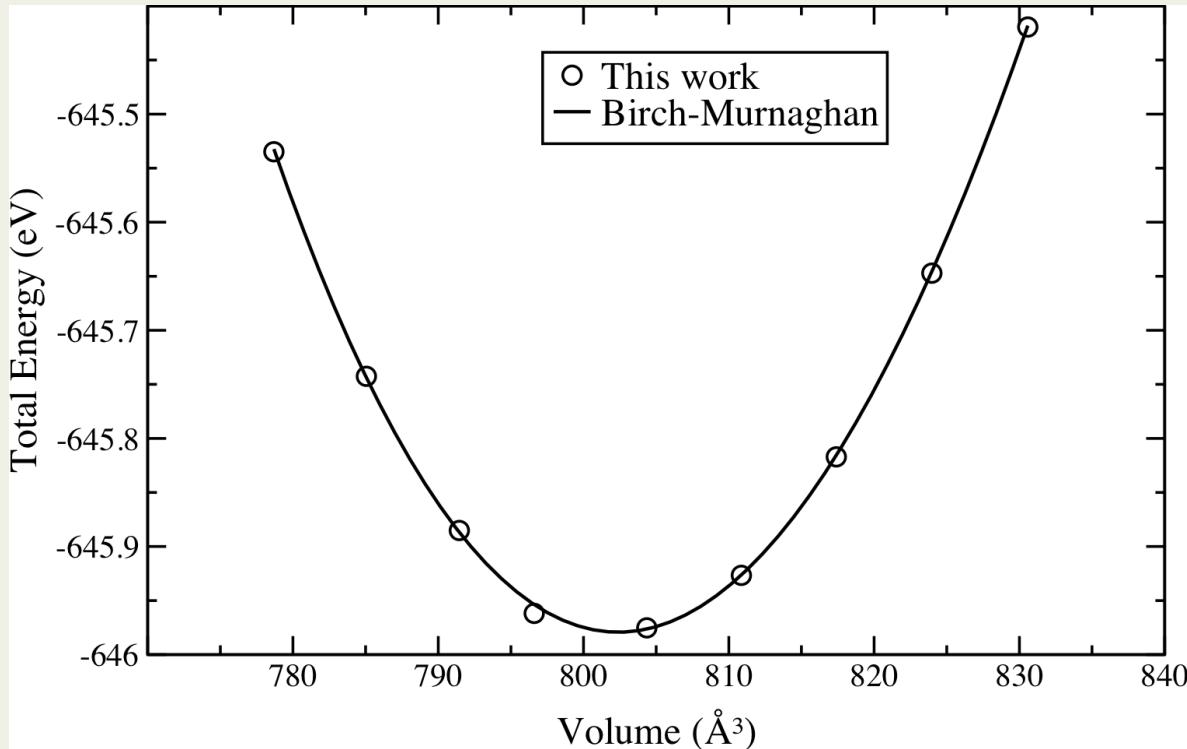


(b)

# Vibrational density of states

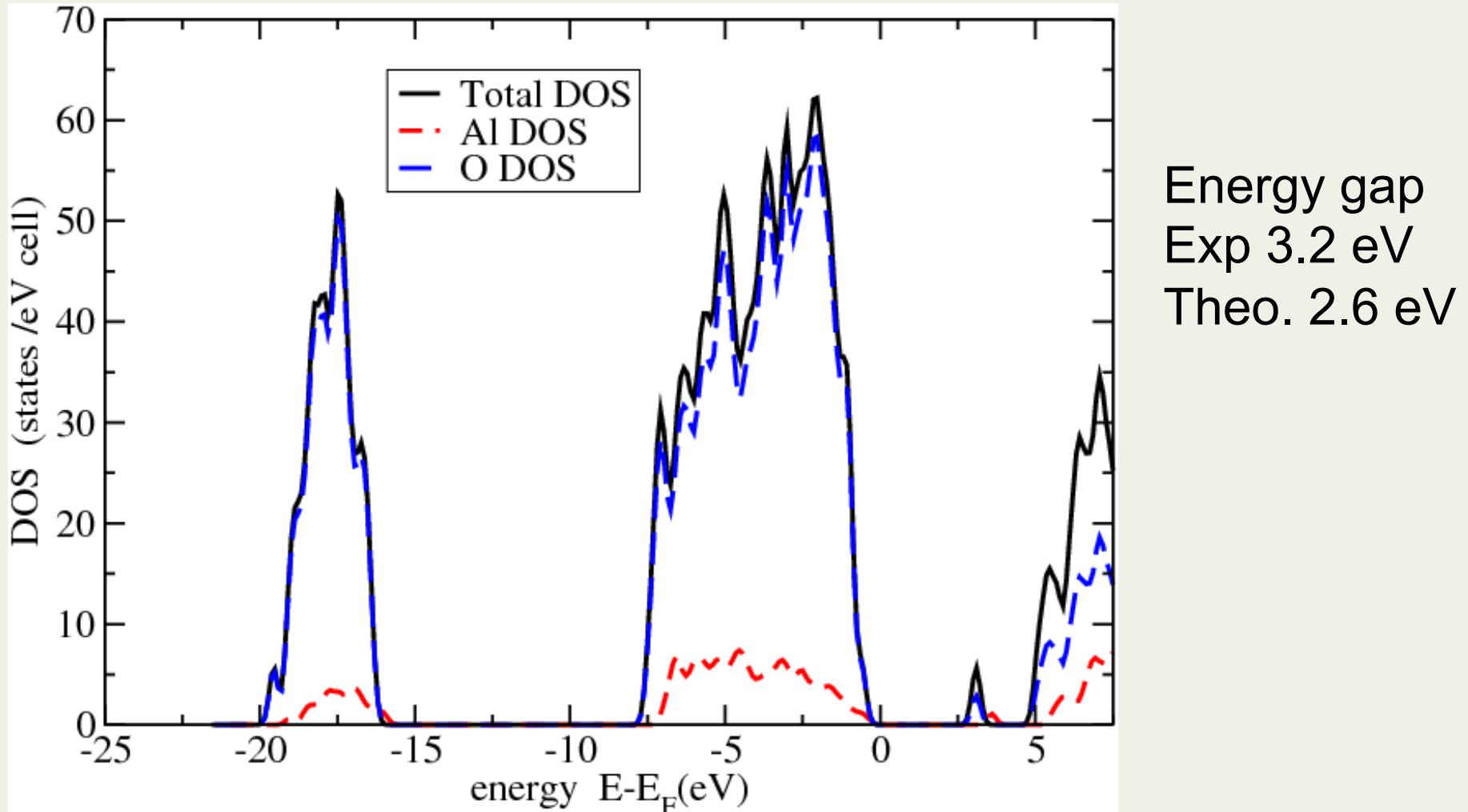


# Elastic properties

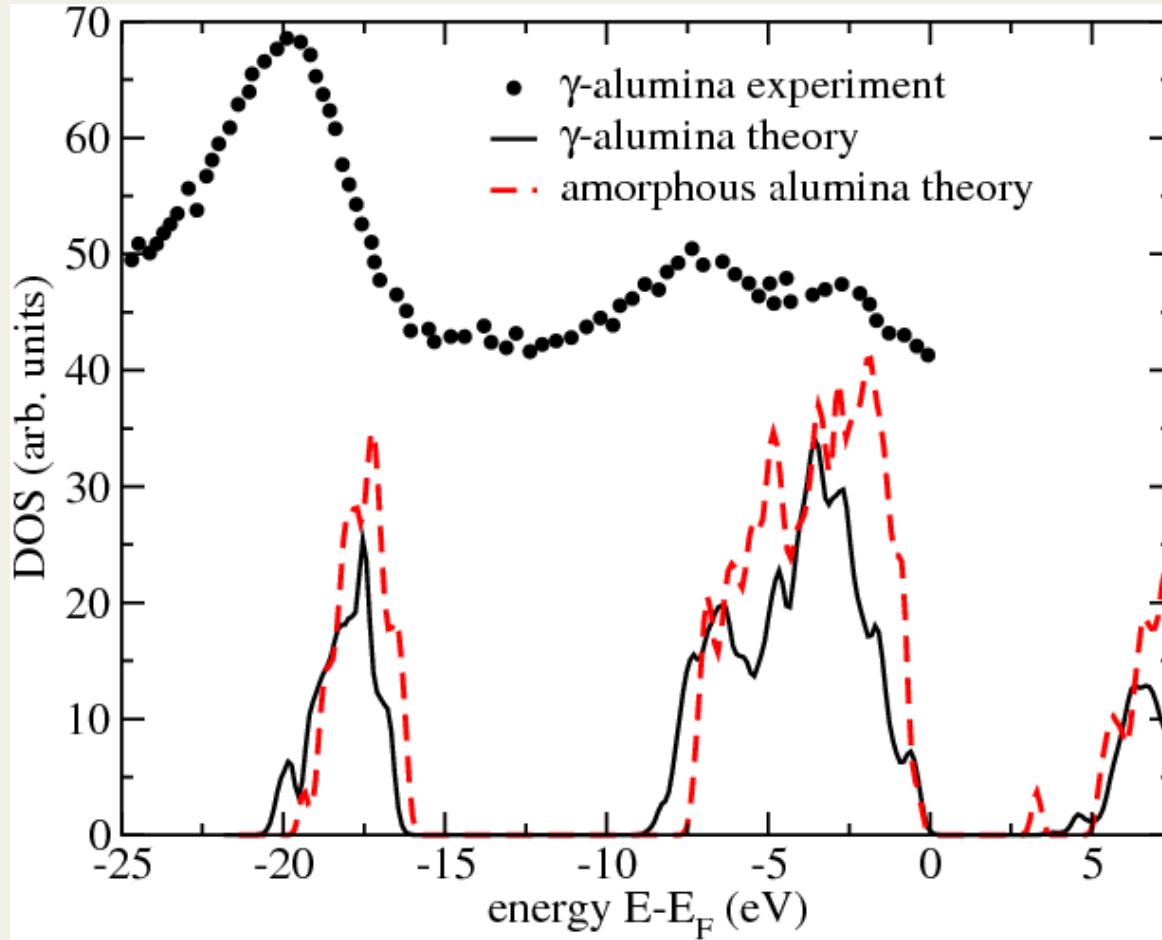


phase	B (GPa)	G (GPa)	E (GPa)	$\nu$
amorph	193.4	141.0	340.3	0.2
Alpha (Wefers & Misra)	253	164	404	0.23

# Electronic density of states



# Electronic density of states: comparison to $\gamma$ -alumina

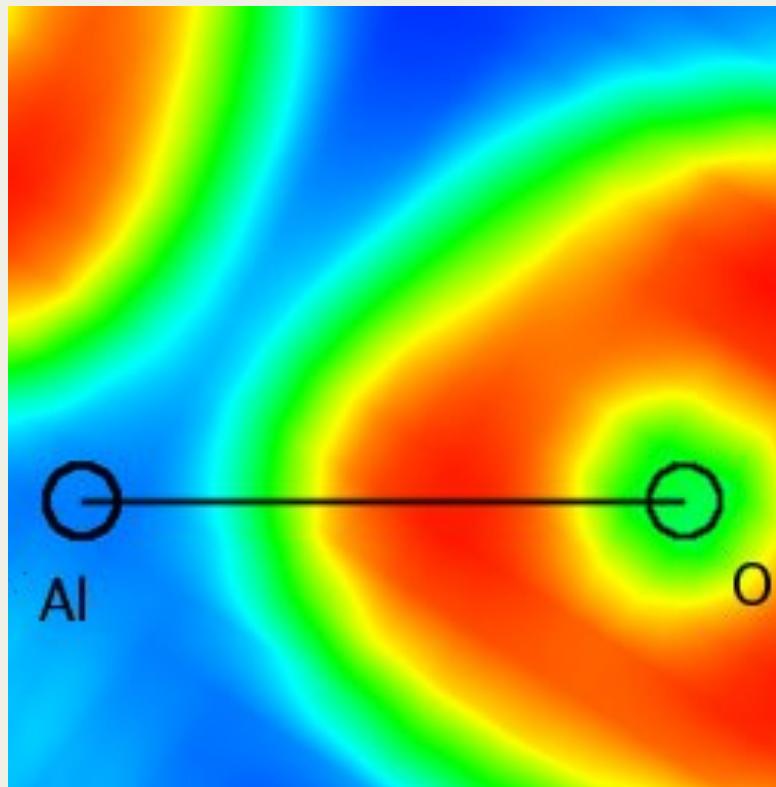


$\gamma\text{-Al}_2\text{O}_3$  Exp: B. Ealet et al. Thin Solid Films **250**, 92 (1994)

Theory: GG, A. Taga. B. Johansson, Phys. Rev. B **65** 012101 (2002)

GG, E. Menéndez, Phys. Rev. B **72** 035116 (2005)

# Electron localization function



Charge transfer  
calculated via  
Voronoi analysis:  
 $\text{Al} \sim 2.89$   
 $\text{O} \sim -1.92$

# Different alumina phases

Phase	Density g/cm <sup>3</sup>	Al Coordination Number	Bond length Al-O (Å)
amorphous <sup>b</sup>	3.17	4(76%), 5 (22%)	1.76
	3.9	4(23%), 5(51%), 6(21%)	1.77
	4.2	4(15%), 5(21%), 6(64%)	1.79
a, ab-initio <sup>d</sup>	3.17	4(50%), 5(42%), 6(5%)	1.81
liquid <sup>a</sup>	3.17	3(13%), 4(66%), 5(20%)	1.76
gamma <sup>e</sup>	3.66	4(37%), 6(63%)	1.94 +/- 0.3
theta	3.65	4(50%), 6(50%)	1.9 +/- 0.3
alpha	3.98	6 (100%)	1.97

Our results:

- a) PRE **61**, 2723 (2000),
- b) PRB **65**, 104202 (2002), unpublished (2008)
- c) PRB **65**, 012101 (2002), PRB, **72**, 035116 (2005)
- d) J. Mat Sc. **45**, 5124–5134 (2010);  
J. Phys.: Condens. Matter **23**, 495401 (2011)

# Conclusions

- Using of ab-initio MD appear new features, absent in (simple) empirical interatomic potential
- The building blocks of the system are  $\text{AlO}_4$  and  $\text{AlO}_6$
- The connectivity of this units is both by the corners (majority) and by the edges (minority)
- The v-DOS present two bands. The low frequency band is related to the inter-unit vibrations, and the high band to the intra-unit vibrations
- $B = 193 \text{ GPa}$ , the lower of all polymorph
- The e-DOS is similar to the one of the crystalline  $\gamma\text{-Al}_2\text{O}_3$ , with a gap of 2.9 eV

# Mechanical properties copper: atomistic simulation

(work in progress)

N. Amigo, GG, M. Ignat

(in the framework of IM2-U. Chile project:  
M. Ignat, A. Valencia, G. Gutiérrez, S. Davis)

# Copper Project

## Determinación de Propiedades Mecánicas de Productos de Cobre

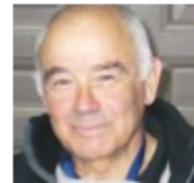
Proyecto CODELCO-IM2 36-11  
Responsable de Proyecto: M.Ignat

Marzo 2012



### Miguel Ignat: Análisis propiedades mecánicas

- Docteur Ingenieur (1977), Docteur en-Sciences (1983)



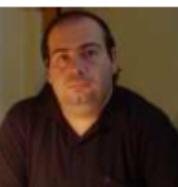
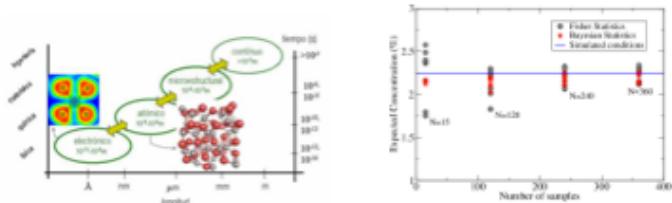
### Álvaro Valencia: Análisis Termodinámico

- Dr.-Ing. Ruhr-Universität Bochum, Alemania, 1993.



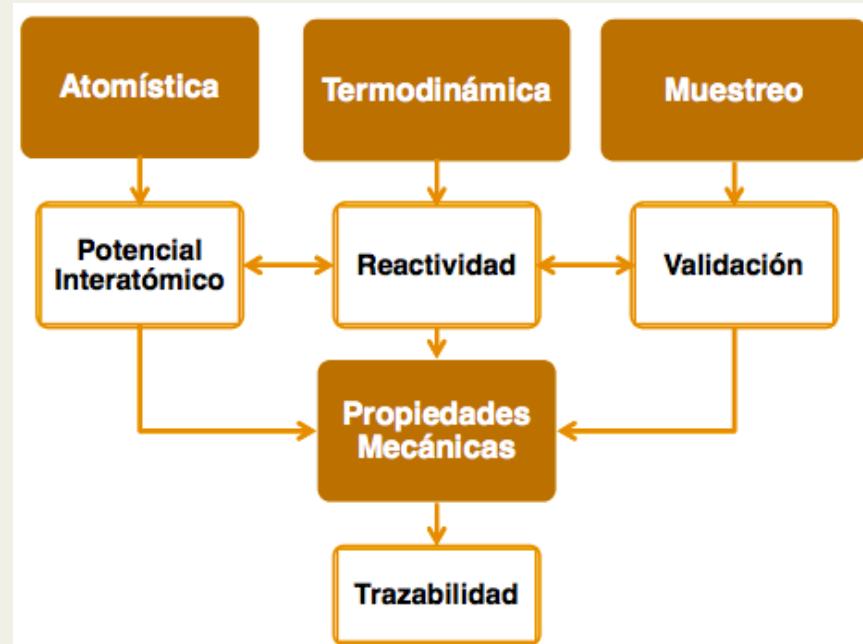
### Gonzalo Gutiérrez: Modelización Atómica

- Doctor en Ciencias con Mención en Física, P. Universidad Católica de Chile, 1997

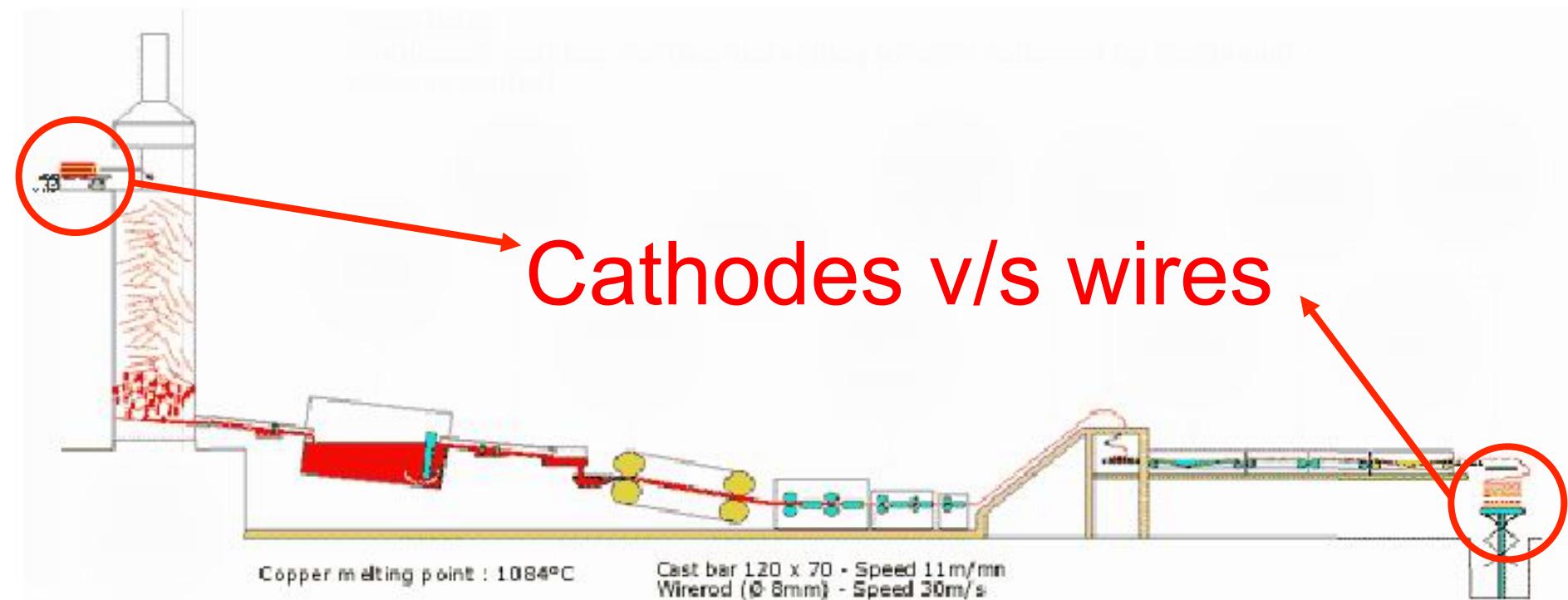


### Sergio Davis: Estadística de Muestreo

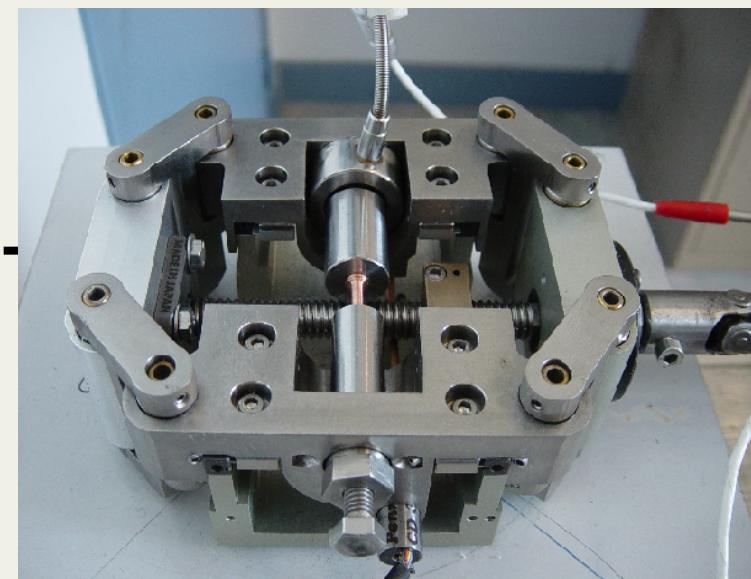
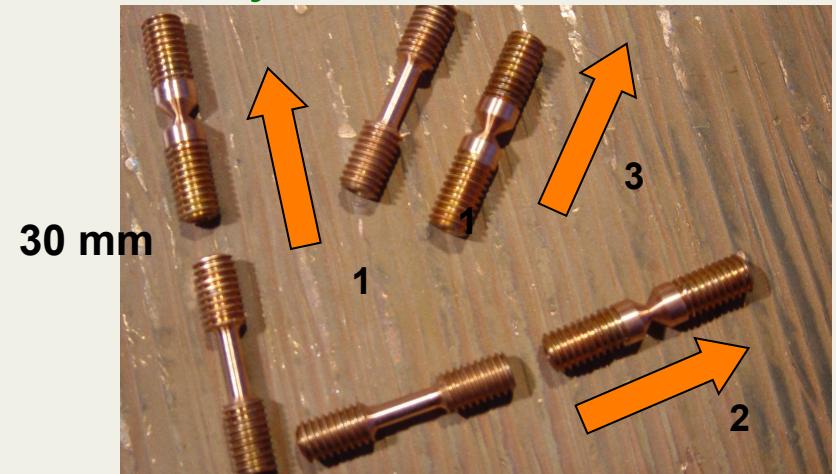
- Ph.D in Applied Material Physics, Royal Institute of Technology (KTH), Estocolmo, Suecia (Septiembre 2009)



# From Cathodes to wires



# Experiments: M. Ignat + Alice Moya and Tomás Jil



mechanical test + analysis → effects of impurities

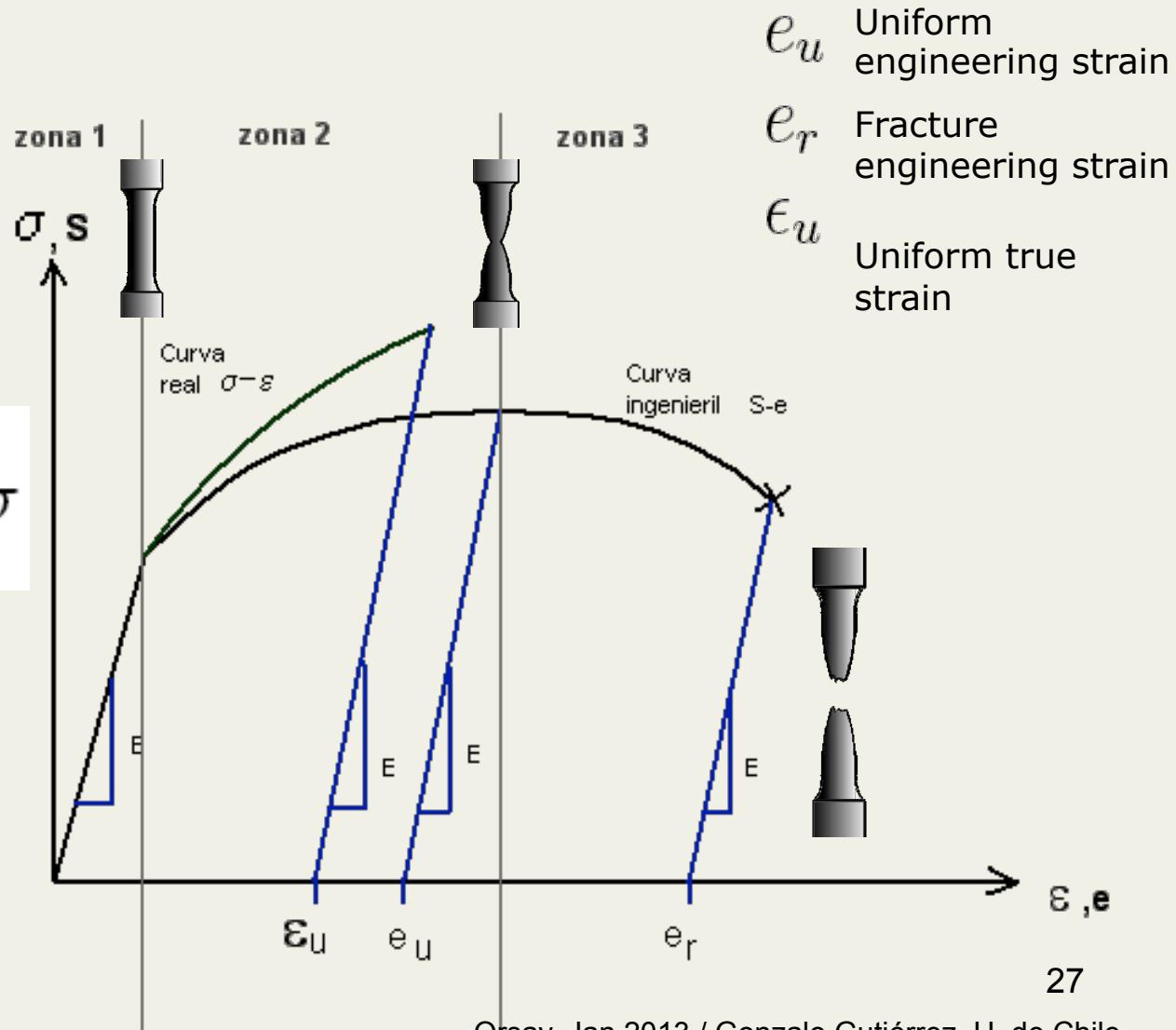
# Tensile test: stress-strain curves

- Ley de Hollomon

$$\sigma = k \epsilon^n$$

$$\frac{dS}{de} = 0 \Rightarrow \frac{d\sigma}{d\epsilon} = \sigma$$

$$\Rightarrow n = \epsilon$$



# Atomistic simulation in Cu

Goal:

to study the effect of impurities in the mechanical behavior of copper, at an atomic level.  
In particular Ag, As, Fe, Pb, S y Cu<sub>2</sub>O

- a) how does the strain-stress curve change due to impurities?
- b) what are the relationship between mechanical properties, impurities and microstructure (grain boundary)?

# Methodology

Classical molecular dynamics

Interatomic potential: embedded atom (many body effect)

Programs: LAMMPS / LPMD (our own code)

Thousands and millions of particles

So far:

Elastic properties

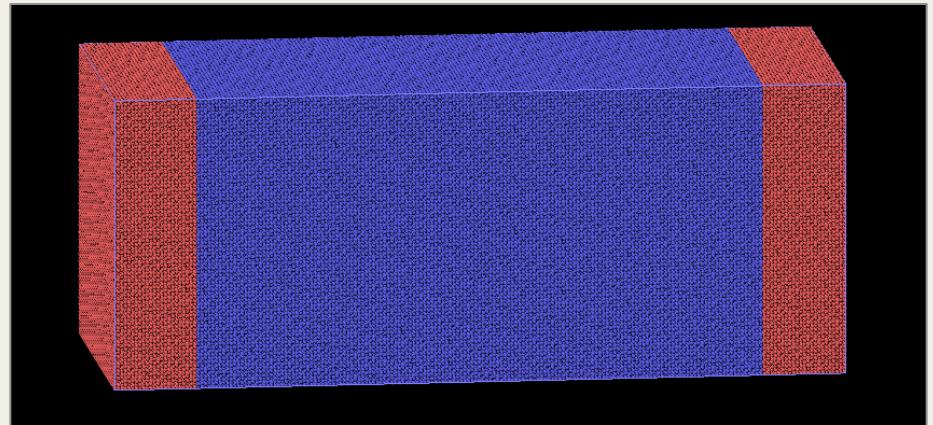
Strain-stress curve

- monocrystal

- polycrystal

# Mono-crystal (T = 0 K)

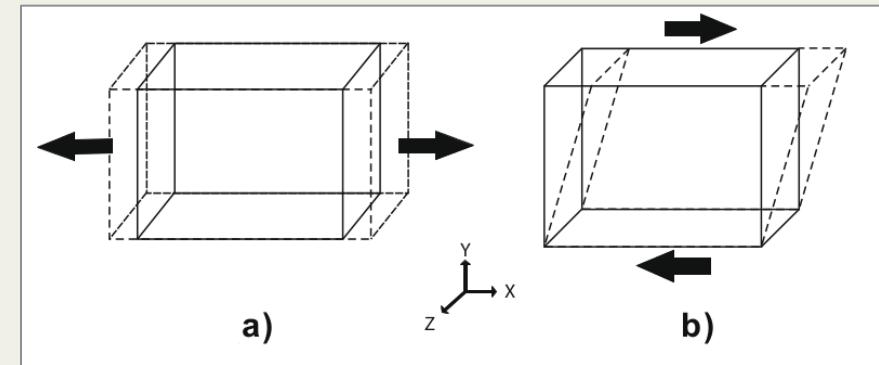
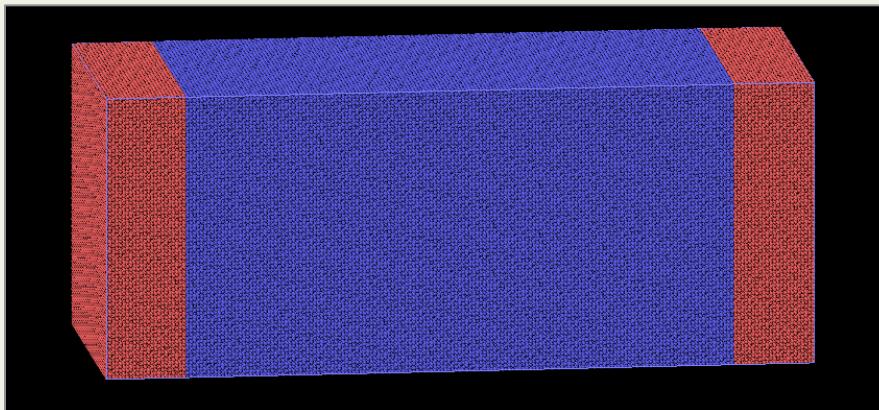
- 660 000 atoms
- 361 [Å] long
- 144 [Å] height and width



# Elastic constants

$$c_{ijkl} = \frac{\partial \sigma_{ij}}{\partial \varepsilon_{kl}}, \quad (i,j,k,l = x,y,z)$$

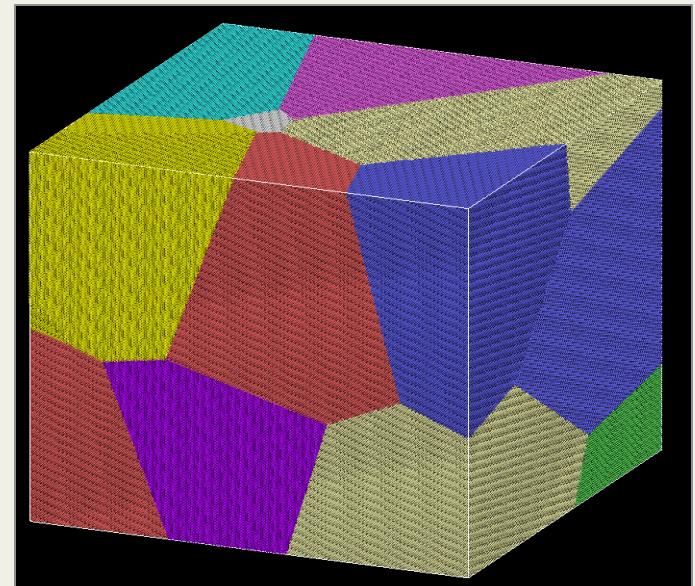
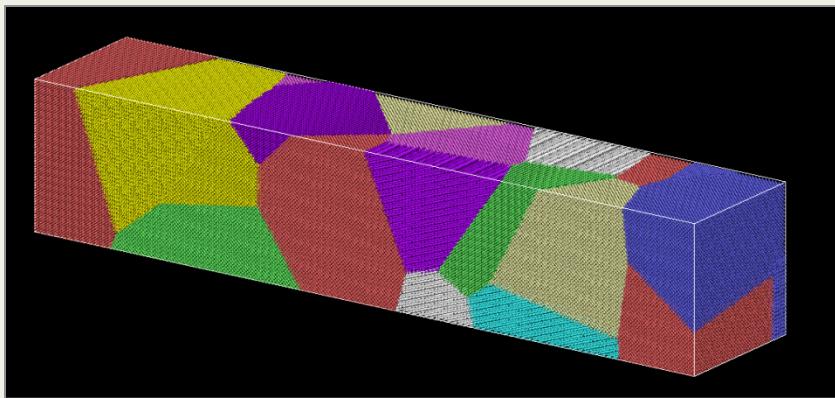
(Elastic properties of the bcc structure of Bismuth at high pressure,, G. Gutiérrez, E. Menéndez-Proupin, and A. K. Singh, Journal of Applied Physics 99, 103504 (2006) )



Constant	Exp [Gpa]	Simulation [Gpa]
$C_{11}$	176.2	171.0
$C_{12}$	125.0	126.3
$C_{44}$	82.0	79.9

# Copper poly-crystals

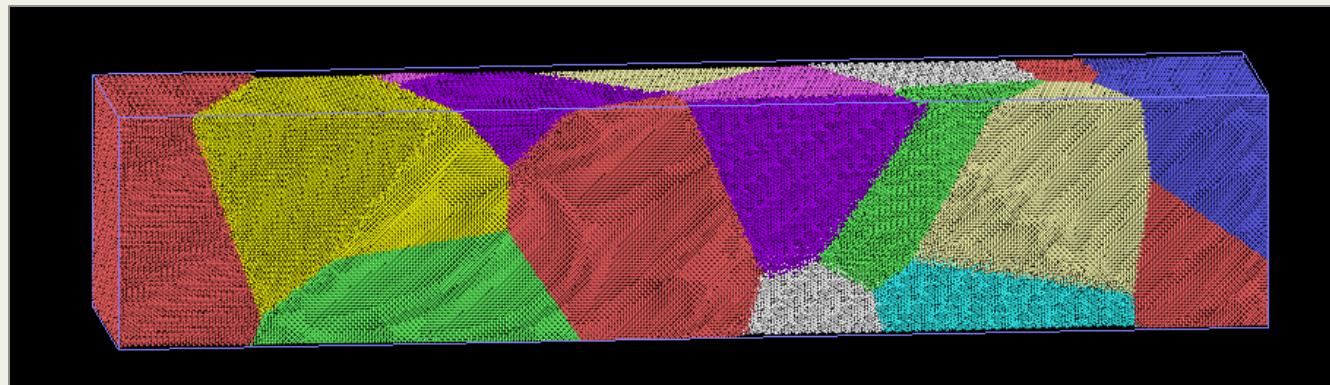
- 1.3 million atoms
- 20 grains
- 722 [Å] long
- 140 [Å] h and w



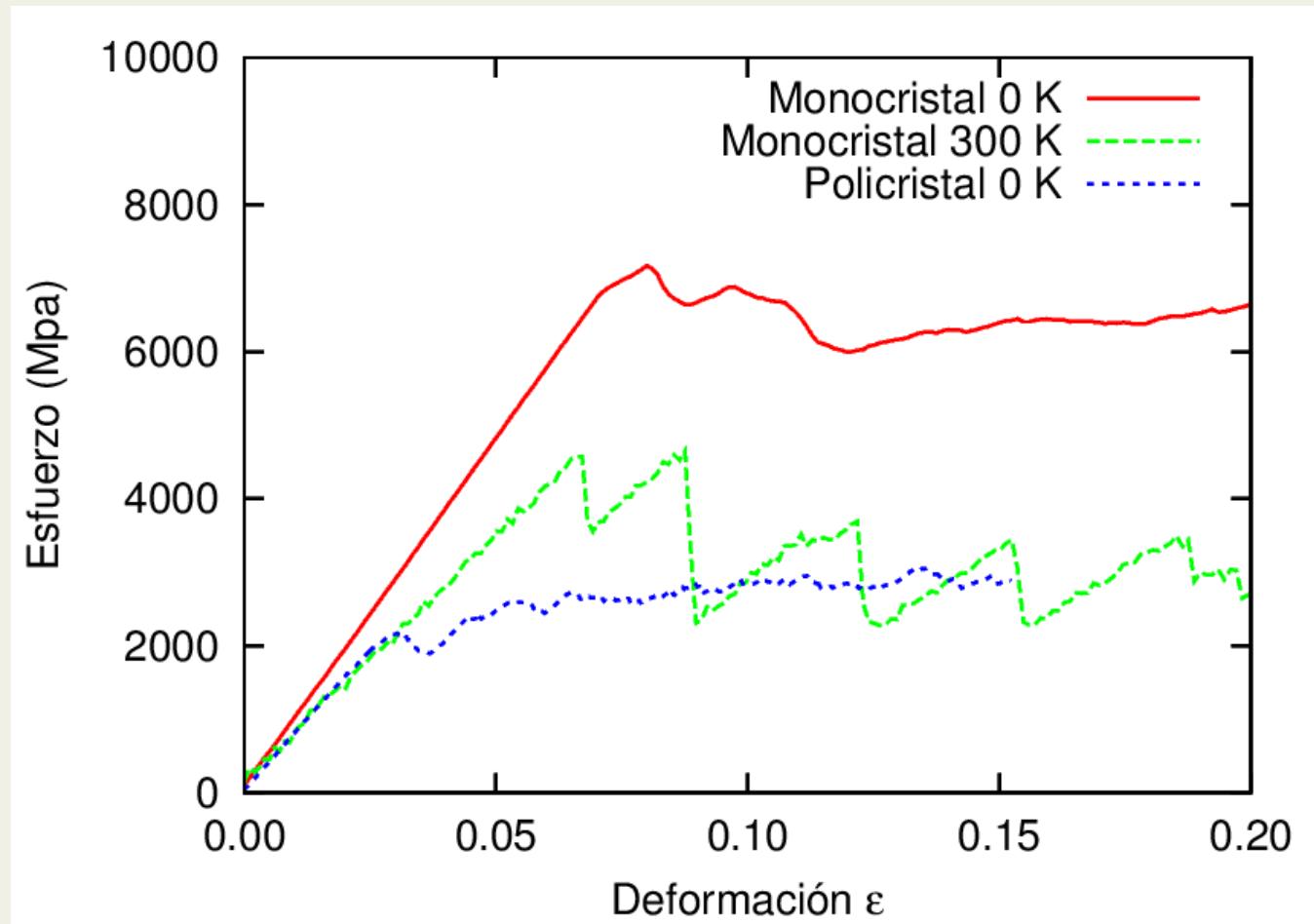
- 20 million
- 20 grains
- 614 [Å] edge

# Poly-cristal

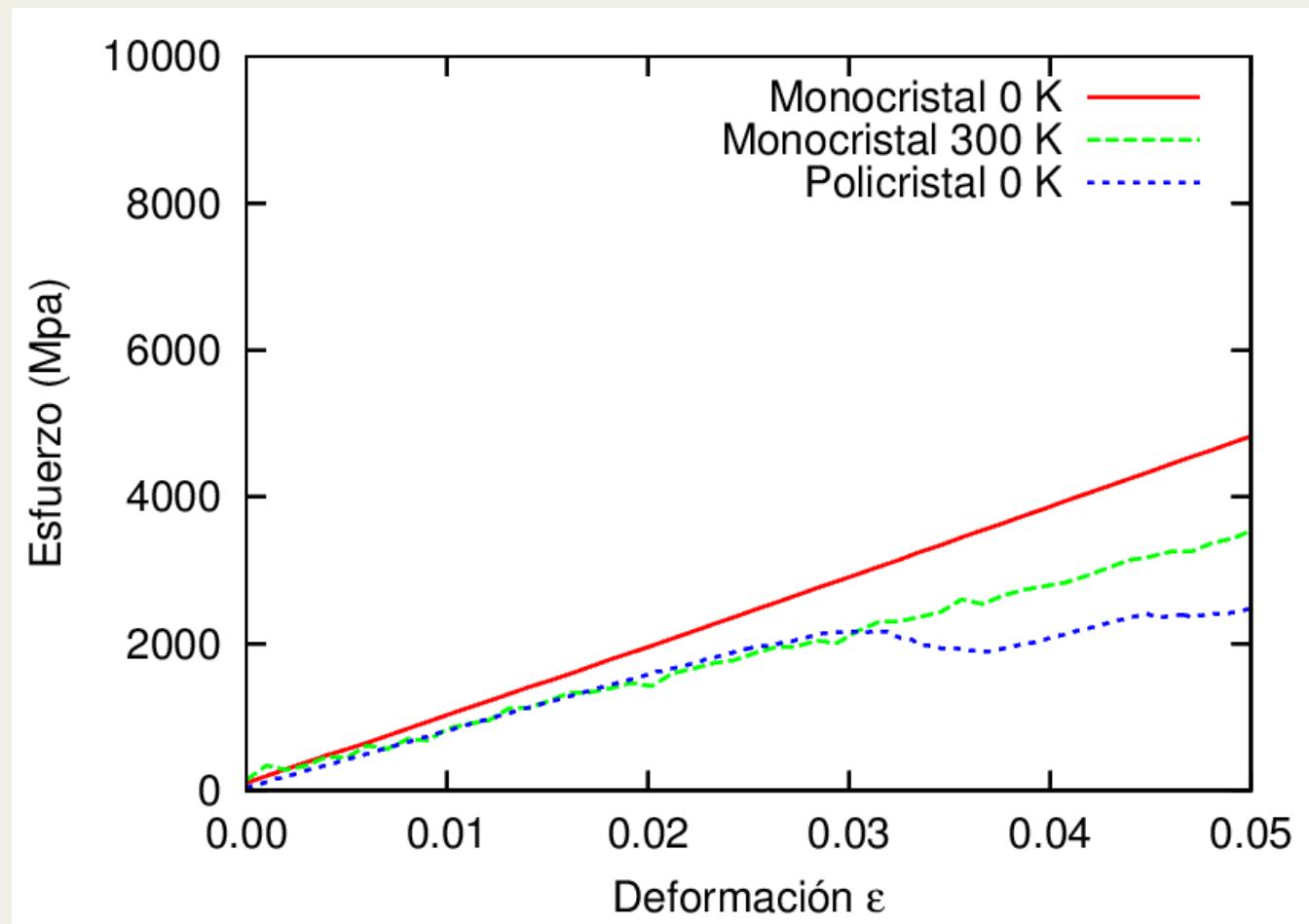
- 1.3 millones de atoms
- 20 grains ( $\sim$ 10-15 nm diameter)
- 720 [Å] l
- 144 [Å] h and w



## Strain-stress test

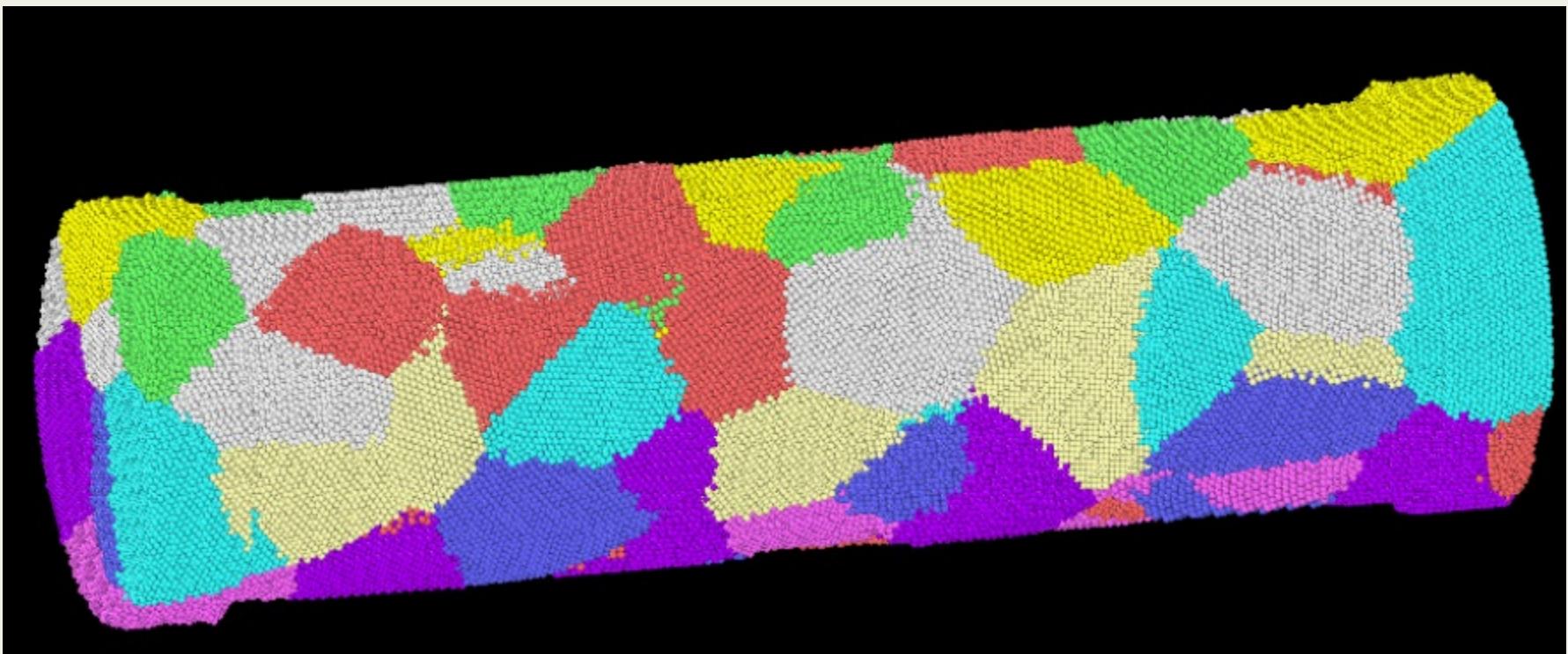


## Zoom at small strain



# Cu and Cu-Ag

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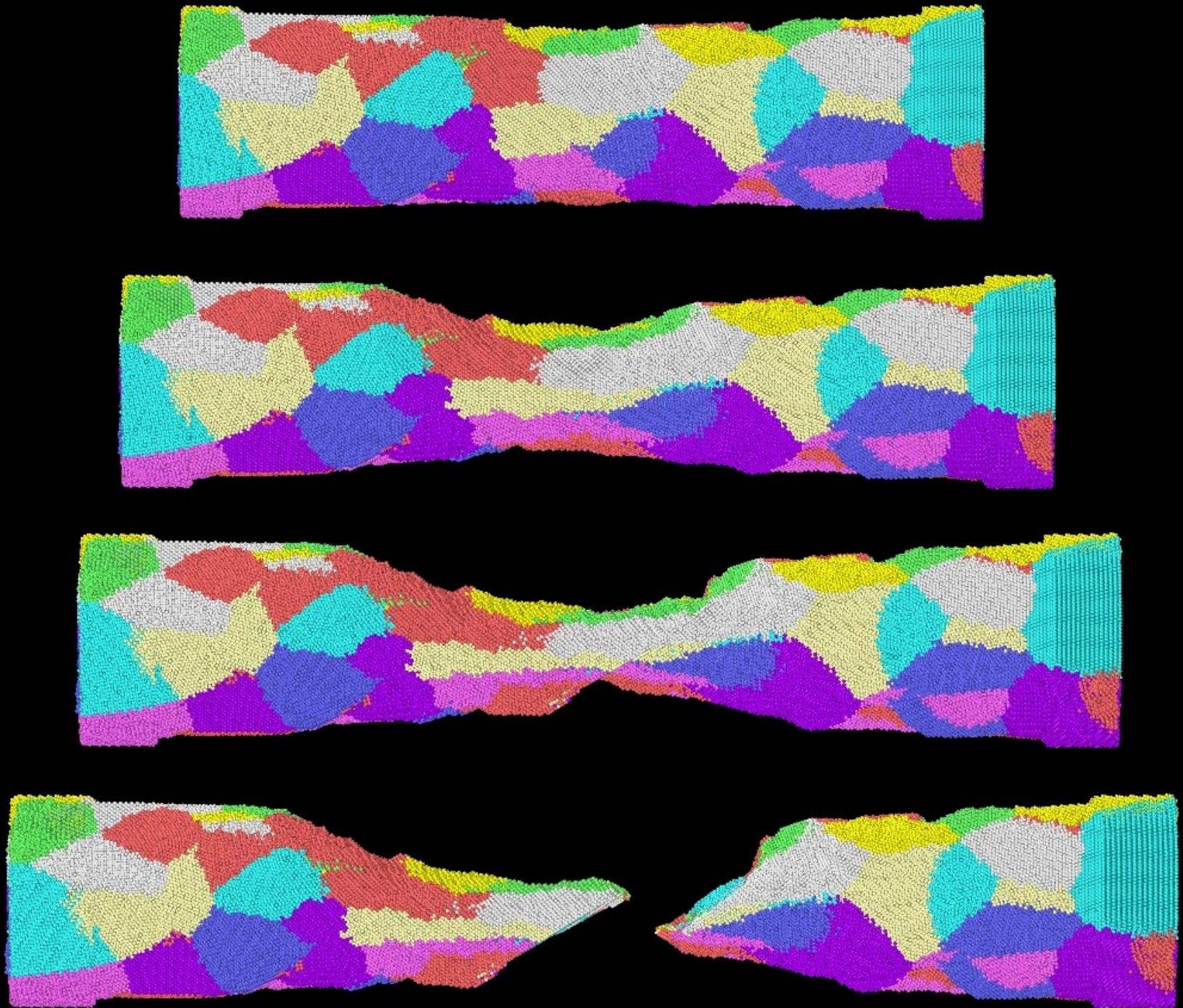


## System 1: pure Cu

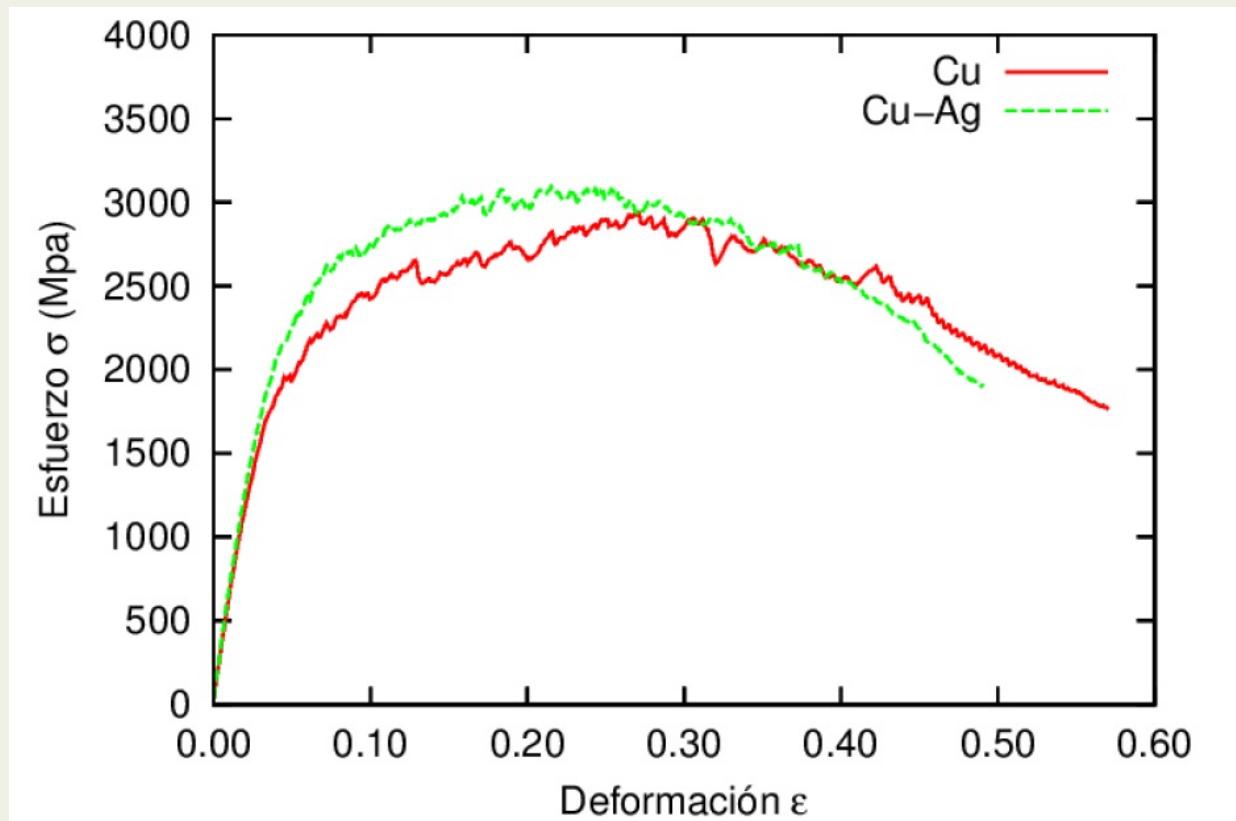
- Cu poly-crystalline cylindrical shape
- 125 grains
- 500 000 atoms approx.
- Long: 470 [Å] , radius: 65 [Å]

## System 2: Cu-Ag

- same as system 1
- Ag interstitial impurities, at concentration of 1.64% (w/r to the total number of atoms)



# Strain-stress curve



Composición	E [GPa]	$\sigma_{elas}$ [MPa]	$\sigma_{ult}$ [MPa]	$\sigma_f$ [MPa]	$\varepsilon_f$
Cu	62.4	1292.7	2924.3	1740.3	0.57
Cu-Ag	67.4	1464.9	3081.4	1876.5	0.49

# Conclusions (preliminary)

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- The strength of poly-crystalline copper increases when Ag interstitials atoms are present
- the tensile strength also increases
- Ag impurities results in a decreases of ductility in Cu.